

PAP Precal

Log Properties

$\log_b x = y$

Properties of Logarithms (only works when $u > 0, v > 0$, and a cannot equal 1)

Logarithm with Base a

Natural Logarithm

Product Property:

$\log_a(uv) = \log_a u + \log_a v$

$\ln(uv) = \ln u + \ln v$

Quotient Property:

$\log_a\left(\frac{u}{v}\right) = \log_a u - \log_a v$

$\ln\left(\frac{u}{v}\right) = \ln u - \ln v$

Power Property:

$\log_a u^n = n \log_a u$

$\ln u^n = n \ln u$

Identity:

$\log_a a = 1$

$\ln e = 1$

$\log_a 1 = 0$

$\ln 1 = 0$

Using Properties of Logarithms

Write each logarithm in terms of $\ln 2$ and $\ln 5$.

1) $\ln 10$

$\ln(2 \cdot 5)$
 $\ln 2 + \ln 5$

2) $\ln \frac{5}{32}$

$\ln 5 - \frac{\ln 32}{5}$
 $\ln 5 - 5 \ln 2$

3) $\log_7 \sqrt[5]{7}$

$\frac{1}{5} \log_7(7)$
 $\frac{1}{5} \log_7 1$
 $\frac{1}{5}(1) = \frac{1}{5}$

4) $3 \ln e^4$

$4 \cdot 3 \ln e$
 12

5) $\log_3 81^{-0.2}$

$\log_3(3^4)^{-0.2}$
 $-0.2 \log_3 3$
 -0.2

This should be blank. This gets glued down!

6) $\log_2(-16)$

Undefined

7) $\ln e^{12} + \ln e^5$

$\ln(e^{12} \cdot e^5)$
 $\ln(e^{17})$

17 $\ln(e)$

17

Rewriting Logarithmic Expressions

Expand each logarithmic expression.

9) $\log 3x^2y$

$\log 3 + \log x^2 + \log y$
 $\log 3 + 2 \log x + \log y$

8) $\log_2 + \log_4 32$

$\log_4(2 \cdot 32)$
 $\frac{\log_4(64)}{\log_4(4^3)}$

3 $\log_4 4$

3

10) $\ln \frac{\sqrt{4x+1}}{8}$

$\ln(4x+1)^{1/2} - \ln 8$
 $\frac{1}{2} \ln(4x+1) - \ln 8$

11) $\log_6 \frac{1}{yz^3}$

$\log_6 1 - \log_6 yz^3$
 $\log_6 1 - (\log_6 y + \log_6 z^3)$
 $\log_6 1 - \log_6 y - 3 \log_6 z$
 $0 - \log_6 y - 3 \log_6 z$
 $-\log_6 y - 3 \log_6 z$

12) $\ln \frac{x^2}{y^3}$

$\ln(x^2)^{1/2} - \ln(y^3)^{1/2}$
 $\ln(x) - \ln(y^{3/2})$
 $\ln x - \frac{3}{2} \ln y$

Condense each logarithmic expression. (Write as a single logarithm and simplify.)

13) $\frac{1}{3} \log x + 5 \log(x-3)$

$\log x^{1/3} + \log(x-3)^5$
 $\log(\sqrt[3]{x} \cdot (x-3)^5)$

14) $4 \ln(x-4) - 2 \ln x$

$\ln(x-4)^4 - \ln x^2$
 $\ln\left(\frac{(x-4)^4}{x^2}\right)$

15) $\frac{1}{5} [\log_3 x + \log_5(x-2)]$

$\frac{1}{5} (\log_3(x(x-2)))$
 $\frac{1}{5} \log_3(x^2-2x)$

$\log_3(\sqrt[5]{x^2-2x})$

16) $\frac{1}{2} [\log_4(x+1) + 2 \log_4(x-1)] + 6 \log_4 x$

$\frac{1}{2} (\log_4((x+1)(x-1)^2)) + \log_4 x^6$
 $\log_4((x+1)(x-1)^2)^{1/2} + \log_4 x^6$
 $\log_4((x+1)^{1/2}(x-1)) + \log_4 x^6$
 $\log_4(\sqrt{x+1} \cdot (x-1)(x^6))$