

1.5 Composition of Functions HW

Given the functions $f(x)$ and $g(x)$ perform the following operations:

1) $f(x) = 2x - 3$ $g(x) = 3x + 5$

a) $(f \circ g)(x)$

$$f(g(x)) \rightarrow f(3x+5)$$

$$2(3x+5) - 3$$

c) $(g \circ f)(3)$

$$g(f(3)) \rightarrow g(2(3)-3) \rightarrow g(3)$$

$$3(3)+5 = \boxed{14}$$

b) $(f \circ g)(0)$

$$f(g(0)) \rightarrow f(3(0)+5)$$

$$f(5) = 2(5) - 3 = \boxed{7}$$

2) $f(x) = \frac{1}{x}$

$g(x) = \frac{1}{x^2}$

a) $(g \circ f)(3)$

$$g(f(3)) \rightarrow g\left(\frac{1}{3}\right) = \frac{1}{\left(\frac{1}{3}\right)^2} = \frac{1}{\frac{1}{9}}$$

$$= \boxed{9}$$

b) $(g \circ f)(x)$

$$g(f(x)) \rightarrow g\left(\frac{1}{x}\right) = \frac{1}{\left(\frac{1}{x}\right)^2} = \boxed{x^2}$$

c) $(f \circ g)(x)$

$$f(g(x)) \rightarrow f\left(\frac{1}{x^2}\right) = \frac{1}{\frac{1}{x^2}} = \boxed{x^2}$$

3) $f(x) = x^2 + x - 12$

$g(x) = |x|$

a) $(f \circ g)(2)$

$$f(g(2)) \rightarrow f(|2|) = f(2)$$

$$2^2 + 2 - 12 = \boxed{-6}$$

b) $(g \circ f)(-7)$

$$g(f(-7)) \rightarrow g((-7)^2 + (-7) - 12)$$

$$g(30) = |30| = \boxed{30}$$

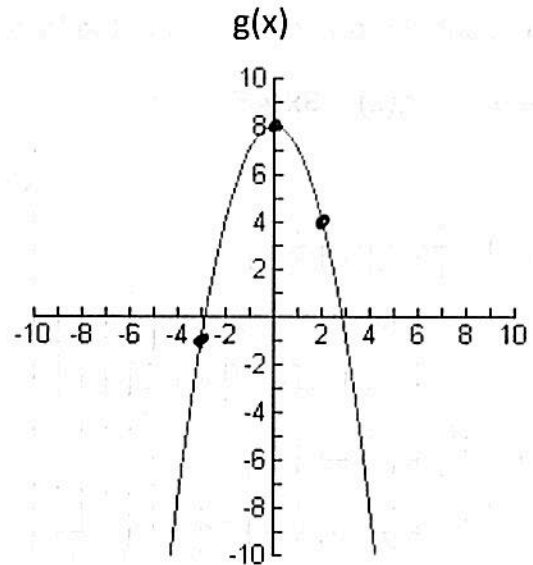
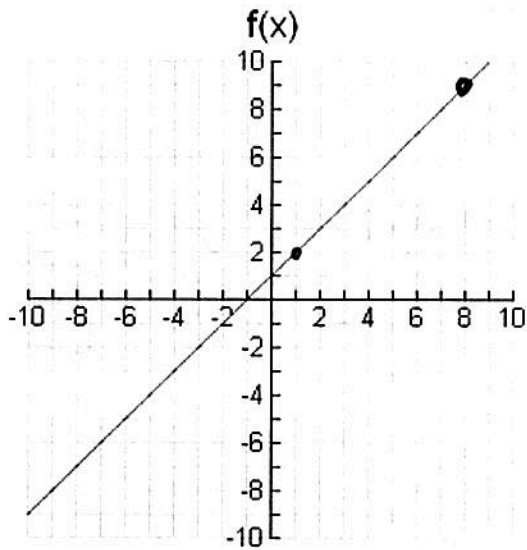
c) $(f \circ g)(x)$

$$f(g(x)) \rightarrow f(|x|)$$

$$\boxed{|x|^2 + |x| - 12}$$

$$\text{or } x^2 + x - 12$$

4. Using the two graphs below, evaluate the following.



a) $f(8) = \boxed{9}$

b) $g(-3) = \boxed{-1}$

c) $g(f(1))$
 $g(2) = \boxed{4}$

d) $f(g(0))$
 $f(8) = \boxed{9}$